# Optimal First-Order Boolean Masking for Embeded loT Devices 

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## Outline

1 Introduction

2 Search Algorithm

3 Applications

4 Compositional Security

5 Conclusion

## Plan

1 Introduction

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## Internet of Things



## Side Channel Attacks

Cryptographic device
(e.g., smart card and reader)


[^0]
## Masking (1/3)

## Countermeasure - masking (first-order example):

- Represent $x \sim\left(r_{x}, x^{\prime}\right)$ such that $x=r_{x} \oplus x^{\prime}$.
- $r_{x}$ is a random bit,
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- Example 1 (XOR):

$$
\begin{aligned}
x & \sim\left(r_{x}, x^{\prime}\right) \\
y & \sim\left(r_{y}, y^{\prime}\right) \\
x \oplus y & \sim\left(r_{x} \oplus r_{y}, x^{\prime} \oplus y^{\prime}\right)
\end{aligned}
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■ Example 2 (AND - Trichina gate):

$$
x \wedge y \sim\left(r_{z}, r_{z} \oplus\left(r_{x} \wedge r_{y}\right) \oplus\left(r_{x} \wedge y\right) \oplus\left(x \wedge r_{y}\right) \oplus(x \wedge y)\right)
$$

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■ $\Rightarrow$ Efficient first-order masking is necessary.

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- AND: Trichina gate. 1 random bit and 8 basic operations.

■ OR: Not studied? Using De Morgan's law and Trichina gate: 1 random bit and 11 basic operations.

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1 fresh random bit required:
■ [+]: masks are always "fresh" $\rightarrow$ easy security proof.

- [-]: PRNG cost.

Our goal: find optimal expressions, without randomness if possible.

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## Interface

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Inputs:

- target Boolean function $t$. For example, AND:

$$
t\left(x_{0}, x_{1}, y_{0}, y_{1}\right)=\left(x_{0} \oplus x_{1}\right) \wedge\left(y_{0} \oplus y_{1}\right)
$$

- number of output shares $m$;
- set of sensitive functions, e.g. $\left\{x_{0} \oplus x_{1}, y_{0} \oplus y_{1}, t\right\}$;

■ set of allowed operations, e.g. $\{X O R, A N D, O R, \underbrace{B I C, O R N}_{A R M-\text { specific }}\}$.

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## Outputs:

- set of $m$ functions $s_{i}$ such that $\bigoplus_{i} s_{i}=t$;
- optimal circuit for computing all $s_{i}$ without first-order leakage of information about sensitive functions.


## The Algorithm (1/3)



- A breadth-first search on sequences of operations.
- A sequence is good if it contains $m$ functions summing to $t$.

■ Several cut-offs involved.

## The Algorithm (2/3)



## Cut-offs:

- First-order leakage check. Leaking sequences are dropped.
- Two sequences with the same set of functions are merged.
- Exploiting share symmetries (swaps, etc.).


## The Algorithm (3/3)

Example of a discovered sequence:
$\neg y_{0}$,
$x_{0} \vee \neg y_{1}$,
$x_{0} \wedge y_{0}$,
$\left(x_{0} \wedge y_{0}\right) \oplus\left(x_{0} \vee \neg y_{1}\right)$,
$x_{1} \vee \neg y_{1}$,
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$x_{1} \wedge y_{0}$,
$\left(x_{1} \wedge y_{0}\right) \oplus\left(x_{1} \vee \neg y_{1}\right)$.
Observe that the sequence contains
$s_{0}=\left(x_{0} \wedge y_{0}\right) \oplus\left(x_{0} \vee \neg y_{1}\right)$,
$s_{1}=\left(x_{1} \wedge y_{0}\right) \oplus\left(x_{1} \vee \neg y_{1}\right)$,
such that
$s_{0} \oplus s_{1}=\left(x_{0} \oplus x_{1}\right) \wedge\left(y_{0} \oplus y_{1}\right)=t$ is the target AND function.

## Results

SecAnd (secure AND):
$z_{0}=\left(x_{1} \wedge y_{1}\right) \oplus\left(x_{1} \vee \neg y_{2}\right)$,
$z_{1}=\left(x_{2} \wedge y_{1}\right) \oplus\left(x_{2} \vee \neg y_{2}\right)$,
Cost: 7 basic / 6 on ARM (versus 8 Trichina gate).
SecOr (secure OR):
$z_{0}=\left(x_{1} \wedge y_{1}\right) \oplus\left(x_{1} \vee y_{2}\right)$,
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No random bits required!

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## Applications

We applied new masking expressions to improve several algorithms:

- Masked Modular Addition/Subtraction by Coron et al. from FSE 2013.
- Masked top 3 64-bit block ciphers in the FELICS benchmarking framework:
- Speck
- Simon
- Rectangle


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- Masked top 3 64-bit block ciphers in the FELICS benchmarking framework:
- Speck
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- Rectangle
- All implementations were checked using Welch's t-test to verify absence of leakage (using simulated traces).
- Just a proof-of-concept to compare performance.
- More work is needed for deployment-ready implementations.


## Kogge-Stone Addition/Subtraction

■ Coron et al. at FSE 2013 proposed masked modular addition algorithm based on the Kogge-Stone adder.

- We used our new expressions together with other modifications.

| Expr. | Time (cycles) |  | Code size (bytes) |  |
| :--- | ---: | ---: | ---: | ---: |
|  | Addition | Subtraction | Addition | Subtraction |
| rolled |  |  |  |  |
| best known | 275 | 388 | 292 | 416 |
| our | 228 | 333 | 232 | 332 |
| gain | $\mathbf{1 7 \%}$ | $\mathbf{1 4 \%}$ | $\mathbf{2 1 \%}$ | $\mathbf{2 0 \%}$ |
| unrolled |  |  |  |  |
| best known | 203 | 296 | 544 | 812 |
| our | 173 | 241 | 480 | 692 |
| gain | $\mathbf{1 5 \%}$ | $\mathbf{1 9 \%}$ | $\mathbf{1 2 \%}$ | $\mathbf{1 5 \%}$ |

## Speck

- Speck: ARX block cipher from NSA.

■ Speck-64/128: 64-bit block, 128-bit key, 27 rounds.

| Expr. | Time (cycles) |  | Code size (bytes) |  |
| :--- | ---: | ---: | ---: | ---: |
|  | Enc | Dec | Enc | Dec |
| rolled adder |  |  |  |  |
| best known | 7131 | 11368 | 340 | 488 |
| our | 5686 | 8258 | 272 | 400 |
| gain | $\mathbf{2 1 \%}$ | $\mathbf{2 7 \%}$ | $\mathbf{2 0 \%}$ | $\mathbf{1 8 \%}$ |
| unrolled adder |  |  |  |  |
| best known | 4945 | 7431 | 588 | 876 |
| our | 4666 | 6188 | 536 | 712 |
| gain | $\mathbf{6 \%}$ | $\mathbf{1 7 \%}$ | $\mathbf{9 \%}$ | $\mathbf{1 9 \%}$ |

## Simon

- Simon: AndRX block cipher from NSA.

■ Simon-64/128: 64-bit block, 128-bit key, 44 rounds.

| Expr. | Time (cycles) |  | Code size (bytes) |  |
| :--- | ---: | ---: | ---: | ---: |
|  | Enc | Dec | Enc | Dec |
| best known | 1736 | 1737 | 152 | 156 |
| our | 1648 | 1649 | 136 | 140 |
| gain | $\mathbf{5 \%}$ | $\mathbf{5 \%}$ | $\mathbf{2 7 \%}$ | $\mathbf{2 5 \%}$ |

## Rectangle

- RECTANGLE: bit-sliced block cipher from academia (Zhang et al.).
■ RECTANGLE-64/128: 64-bit block, 128-bit key, 25 rounds.

| Expr. | Time (cycles) |  | Code size (bytes) |  |
| :--- | ---: | ---: | ---: | ---: |
|  | Enc | Dec | Enc | Dec |
| best known | 3661 | 3442 | 632 | 444 |
| our | 2584 | 2954 | 564 | 372 |
| gain | $\mathbf{1 9 \%}$ | $\mathbf{1 4 \%}$ | $\mathbf{1 1 \%}$ | $\mathbf{1 6 \%}$ |

## First-Order Masking Penalty



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Unfortunately, no! A simple counterexample by a reviewer:

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Using our expressions to mask this circuit results in a first-order leakage.
Problem: dependent input masks to SecAnd.

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Problem: dependent input masks to SecAnd.
Solution: ... remask! But not after each operation.

## Compositional Security (2/3)

How often to remask?

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How often to remask?
Consider for example SecAnd:

$$
\left(z^{\prime}, r_{z}\right)=\operatorname{Sec} A n d\left(\left(x^{\prime}, r_{x}\right),\left(y^{\prime}, r_{y}\right)\right)
$$

After simplification, we have:

$$
\begin{aligned}
& z^{\prime}=z \oplus r_{x} y \oplus r_{y} \oplus 1, \\
& r_{z}=r_{x} y \oplus r_{y} \oplus 1
\end{aligned}
$$

Observe that $r_{z}$ is linear in $r_{x}$ and $r_{y}$. However, the expression depends on the secret variable $y$. Similar proposition holds for SecOr as well.

## Compositional Security (3/3)

■ We can track the coefficient vector of each share through the circuit.

- For example:
- Consider 4 random shares $r_{0}, \ldots, r_{3}$.
- Consider the random mask: $r_{0} \oplus x r_{1} \oplus r_{2}$.
- We represent it as ( 1, ?, 1,0 ).
- SecAnd / SecOr are secure if the input vectors are independent.
- If the known vector coefficients of the shares match, we remask the shares before the operation.
■ Otherwise masks are guaranteed to be independent.
- Requires case-by-case study - future work.


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## Conclusion

■ New, optimal expressions for first-order masking.

- Decrease penalty of protecting lightweight block ciphers.

Open problems:

- Optimal remasking frequency?


## Thank you!


[^0]:    ${ }^{1}$ Credit: wikipedia

